

Car driving up hill with rear wheel drive, Torque from motor applied to rear axle.

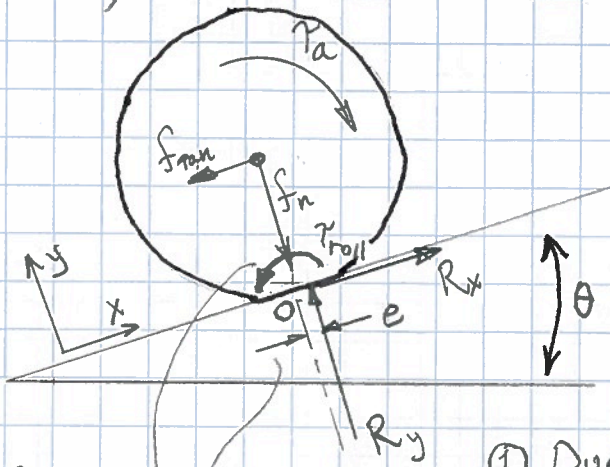
Assume mg is evenly split between front, rear axles.

θ = hill angle

v = car velocity = $r_{\text{wheel}} \cdot \omega$
 mg = car weight

τ_a = Torque from motor about rear axle.

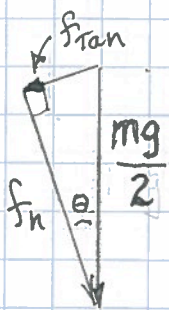
Detail, FBD rear wheel:



$$f_n = \frac{1}{2} mg \cos \theta$$

$$f_{\text{tan}} = \frac{1}{2} mg \sin \theta$$

τ_{roll} = Tire rolling resistance Torque = $R_y \cdot e$



equivalent, (don't "double count")

① Due to rolling resistance, R_y is not exactly beneath f_n ; it is slightly toward front of contact area, by amount "e".

② R_x is the Traction force required to climb uphill. Note: $R_x \leq \mu f_n$

R_x is not part of P_{loss} !

$$\sum F_x: R_x - f_{\text{tan}} = 0 \quad \sum F_y: R_y - f_n = 0$$

$$\sum M_o: -\tau_a + \tau_{\text{roll}} + f_{\text{tan}} \cdot r_{\text{wheel}} = 0 \quad \text{or}$$

$$\tau_a = f_{\text{tan}} \cdot r_{\text{wheel}} + \tau_{\text{roll}}, \quad \text{where } \tau_{\text{roll}} = R_y \cdot e$$

$$\text{Power: } \underbrace{\tau_a \cdot \omega}_{P_{\text{in}}} = \underbrace{f_{\text{tan}} \cdot r_{\text{wheel}} \cdot \omega}_{P_{\text{climb}}} + \underbrace{\tau_{\text{roll}} \cdot \omega}_{P_{\text{loss}}}$$